

#11

Thermochemistry Problem Set

Problem 1

An average hot water tank will hold 300.0 L of water needs to be kept at 65.0°C in order to kill any bacteria in the water. If you are filling a new tank with water at a starting temperature of 12.5°C, what mass of natural gas (methane) must be burned in a complete combustion reaction in order bring your tank up to the correct temperature?



① find ΔH_r° using enthalpy of formation

$$\begin{aligned}\Delta H_r^\circ &= (\Delta H_f^\circ \text{CO}_2(g) + 2\Delta H_f^\circ \text{H}_2\text{O}(g)) - (\Delta H_f^\circ (\text{CH}_4)_g) \\ &= [-393.5 + 2(-241.8) - (-74.6)] \\ &= -802.5 \text{ kJ}\end{aligned}$$

② $Q_{\text{water}} = 300000 \text{ g} \times 4.184 \frac{\text{J}}{\text{g}^\circ\text{C}} \times 52.5^\circ\text{C}$

$\begin{matrix} 65.0 \\ -12.5 \end{matrix}$

$\begin{matrix} 300.0 \text{ L} \\ \times 1.0 \frac{\text{g}}{\text{mL}} \times 1000 \frac{\text{mL}}{\text{L}} \end{matrix}$

$= 65898000 \text{ J or } 65898 \text{ kJ}$

③ $\Delta H = -Q_{\text{sur}} = -65898 \text{ kJ}$

④ $\frac{\Delta H_1}{n_1} = \frac{\Delta H_2}{n_2} \Rightarrow \frac{-65898 \text{ kJ}}{x \text{ mol}} = \frac{-802.5 \text{ kJ}}{1 \text{ mol}}$

$x = \frac{-65898}{-802.5}$

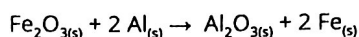
$x = 82.116 \text{ mol}$

⑤ $\begin{aligned}\text{mass} &= n \times M \\ &= 82.116 \text{ mol} \times 16.04 \frac{\text{g}}{\text{mol}} \\ &= 1317.1 \text{ g}\end{aligned}$

Correct to 3 sig fig $\Rightarrow 1320 \text{ g}$ of CH_4 is needed

Problem 2

The Thermite reaction can be used to produce molten iron for welding railway tracks together.



Calculate the amount of heat produced using 45.0 g of aluminum and excess iron (III) oxide.

$$\begin{aligned} \textcircled{1} \Delta H_r^\circ &= [\Delta H_f^\circ \text{Al}_2\text{O}_{3(s)}] - [\Delta H_f^\circ \text{Fe}_2\text{O}_{3(s)}] \\ &= -1675.7 - (-824.2) \\ &= -851.5 \text{ kJ} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \text{mol Al} &= 45.0 \text{ g} \times \frac{1 \text{ mol}}{26.98 \text{ g}} \\ &= 1.6679 \text{ mol} \end{aligned}$$

$$\textcircled{3} \frac{\Delta H_1}{n_1} = \frac{\Delta H_2}{n_2}$$

$$\frac{-851.5 \text{ kJ}}{2 \text{ mol Al}} = \frac{x}{1.6679 \text{ mol}}$$

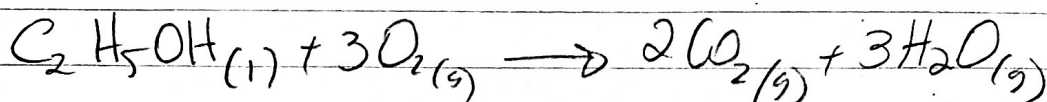
Mole Coefficient in balanced equation

$$\begin{aligned} x &= \frac{-851.5 \times 1.6679}{2} \\ &= -710.1 \text{ kJ} \\ 3 \text{ sig fig} &\Rightarrow \{-7.10 \times 10^2 \text{ kJ}\} \end{aligned}$$

#3

Problem 3

It's 1976 and you are throwing a fondue party! You need to heat 800.0 mL of vegetable oil to 375°F (190.0°C) using an ethanol burner. Assuming a perfect transfer of heat from the burner into the oil, what mass of ethanol is required? Assume your kitchen is at SATP, vegetable oil has a density of 0.920 g/mL and the specific heat capacity of vegetable oil is 2.000 J/g•°C



$$\textcircled{1} \quad Q = mc\Delta T$$

$$\text{oil} = 736 \times 2.000 \times 165 = 242880 \text{ J}$$

$$m_{\text{oil}} = 800.0 \text{ mL} \times 0.920 \text{ g/mL} = 736 \text{ g}$$

$$\textcircled{2} \quad \Delta H_{\text{system}} = -242880 \text{ J} = -242.880 \text{ kJ}$$

$$\Delta T = 190.0^\circ - 25^\circ = 165^\circ \text{C} \quad \uparrow_{\text{SATP}}$$

③ find ΔH_r° using ΔH_f°

$$\Delta H_r^\circ = [2\Delta H_f^\circ \text{CO}_{2(g)} + 3\Delta H_f^\circ \text{H}_2\text{O}_{(g)}] - [\Delta H_f^\circ \text{C}_2\text{H}_5\text{OH}_{(l)}]$$

$$= [2(-393.5) + 3(-241.8)] - [(-277.6)]$$

$$= -1234.8 \text{ kJ}$$

$$\textcircled{4} \quad \frac{\Delta H_1}{n_1} = \frac{\Delta H_2}{n_2}$$

$$\frac{-1234.8 \text{ kJ}}{1 \text{ mol}} = \frac{-242.880 \text{ kJ}}{n_2}$$

Found in steps 1 + 2

Mol coefficient in Balanced equation for ethanol

$$n_2 = 0.197 \text{ mol}$$

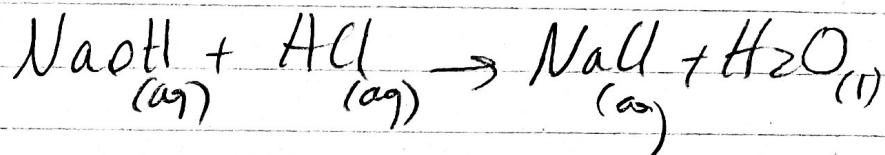
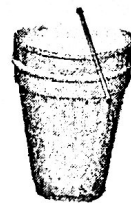
$$\textcircled{5} \quad m = n \times M \Rightarrow n = 0.197 \text{ mol} \times 46.08 \text{ g/mol} = 9.08 \text{ g}$$

2 sig. fig. = 9.1 g

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Problem 4

100.0 mL of 3.0 M HCl can be neutralized with exactly 200.0 mL of 1.5 M NaOH. If this reaction is done in a coffee cup calorimeter, what temperature change would you expect to observe?



$$\begin{aligned} \textcircled{1} \Delta H_r^\circ &= [\Delta H_f^\circ \text{NaCl}_{(aq)} + \Delta H_f^\circ \text{H}_2\text{O}_{(l)}] - [\Delta H_f^\circ \text{NaOH}_{(aq)} + \Delta H_f^\circ \text{HCl}] \\ &= (-411.2 + (-285.8)) - (-92.3 + (-425.6)) \\ &= -179.1 \text{ kJ} \end{aligned}$$

$$\textcircled{2} \frac{\Delta H_1}{n_1} = \frac{\Delta H_2}{n_2}$$

Note: $\text{mol}_{\text{NaOH}} = \text{mol}_{\text{HCl}}$
both reacting completely

$$\frac{-179.1 \text{ kJ}}{1 \text{ mol NaOH}} = \frac{x \text{ kJ}}{0.30 \text{ mol}}$$

$$x = -53.73 \text{ kJ}$$

$$\textcircled{3} Q_{\text{sur}} = +53.73 \text{ kJ} \text{ or } 53730 \text{ J}$$

$$\textcircled{4} Q = mc \Delta T$$

$$53730 \text{ J} = 300.0 \text{ g} \times 4.184 \frac{\text{J}}{\text{g}^\circ\text{C}} \times \Delta T$$

$$\Delta T = 42.8^\circ\text{C}$$

$$2 \text{ sig. fig.} \Rightarrow 43^\circ\text{C}$$

Problem 5

A lab technician places 5.00 g of Doritos (2 chips) into a bomb calorimeter with a heat capacity of 9.23 kJ/°C. The initial temperature of the calorimeter system is 21.0°C. After burning the food, the final temperature of the system is 32.0°C. How much thermal energy is released by the combustion of the food in kilojoules per gram?



Follow-up question!

Calories on food packages are actually kilocalories (kcal). If 1 kJ = 0.2388 kcal, what is the caloric value of a 45 g bag?

$$Q = mc\Delta T \quad \text{or} \quad Q = C \times \Delta T$$

they gave us 9.23 kJ/°C

$$Q = 9.23 \frac{\text{kJ}}{^\circ\text{C}} \times 11.0^\circ\text{C}$$

$$= 101.53 \text{ kJ}$$

$$\Delta H_{\text{sys}} = -101.53 \text{ kJ}$$

$$\frac{\text{kJ}}{\text{g}} \Rightarrow \frac{-101.53 \text{ kJ}}{5 \text{ g}}$$

$$= 20.3 \text{ kJ/g}$$

$$20.3 \frac{\text{kJ}}{\text{g}} \times \frac{0.2388 \text{ kcal}}{1 \text{ kJ}}$$

$$= 4.85 \text{ kcal/g}$$

$$\text{Food sample} = 45 \text{ g} \quad \therefore 4.85 \frac{\text{kcal}}{\text{g}} \times 45 \text{ g} \\ = 218 \text{ kcal}$$